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**More Evidence On
“Which Panel Data Estimator Should I Use?”**

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WORKING PAPER

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3 September 2016

Abstract: This study uses Monte Carlo experiments to produce new evidence on the performance of a wide range of panel data estimators. It focuses on estimators that are readily available in statistical software packages such as Stata and Eviews, and for which the number of cross-sectional units (N) and time periods (T) are small to moderate in size. The goal is to develop practical guidelines that will enable researchers to select the best estimator for a given type of data. It extends a previous study on the subject (Reed and Ye, 2011), and modifies their recommendations. The new recommendations provide a (virtually) complete decision tree: When it comes to choosing an estimator for efficiency, it uses the size of the panel dataset (N and T) to guide the researcher to the best estimator. When it comes to choosing an estimator for hypothesis testing, it identifies one estimator as superior across all the data scenarios included in the study. An unusual finding is that researchers should use different estimators for estimating coefficients and testing hypotheses. We present evidence that bootstrapping allows one to use the same estimator for both.

Keywords: Panel Data Estimators, Monte Carlo simulation, PCSE, Parks model, Bootstrapping

JEL Classifications: C23, C33

Acknowledgements: We acknowledge helpful comments from conference participants at the 2016 New Zealand Econometric Study Group meetings, and the 2016 New Zealand Association of Economists meetings. All remaining errors are ours.

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I. INTRODUCTION

For applied researchers using panel data, there is an abundance of possible estimators one can choose. A key issue is how one decides to handle cross-sectional dependence. There are three general approaches. One approach is to model the error-variance covariance matrix in the framework of Seemingly Unrelated Regression (SUR). Here the common estimator is Feasible Generalized Least Squares (FGLS), where the cross-sectional covariances are typically modelled parametrically. The classic reference is Parks (1967) and the corresponding data-generating process (DGP) is commonly called the Parks model. This is the underlying statistical model for Stata's *xtgls* procedure. A major problem with this approach is the large number of parameters that need to be estimated.

An alternative approach is to model the cross-sectional dependencies “spatially” (Anselin, 2013; Baltagi et al., 2013; Elhorst, 2014; Bivand and Piras, 2015). This typically involves modelling the dependencies across units as a function of distance, in either a continuous or binary fashion. While this has the advantage of greatly reducing the number of parameters to be estimated, it comes at the cost of possible misspecification. Misspecification occurs if the nature of the respective cross-sectional dependencies cannot be effectively reduced to a function of distance (Corrado and Fingleton, 2012).

Another alternative is to model cross-sectional correlation as a function of time-specific common factors (Pesaran and Smith, 1995; Bai, 2003; Coakley et al., 2006; Pesaran, 2006; Eberhardt et al., 2013; Kapetanios et al., 2011). This approach has proven particularly popular in the macro panel literature (Eberhardt and Teal, 2011). While the multi-factor framework for cross-sectional correlation allows one to incorporate a number of other important issues, it also comes at the cost of possible misspecification, because it also greatly reduces the number of parameters to be estimated.

In this context, it is useful to consider the classic Parks model in greater detail. In its general form, with groupwise heteroskedasticity, group-wise specific AR(1) autocorrelation, and time-invariant cross-sectional correlation, the Parks model has a total of $\left(\frac{N^2+3N}{2}\right)$ unique parameters in the error variance-covariance matrix (EVCN), where N is the number of cross-sectional units. This causes two problems. First, the FGLS estimator cannot be estimated when the number of time periods, T , is less than N , because the associated EVCN cannot be inverted (Beck and Katz, 1995). To estimate FGLS in this setting, one needs to restrict the number of elements in the EVCN. Second, even when $T \geq N$, there may be relatively few observations per EVCN parameter, causing the associated elements of the EVCN to be estimated with great imprecision. As demonstrated by Beck and Katz (1995), henceforth BK, this can cause severe underestimation of coefficient standard errors, rendering hypothesis testing useless.

Despite these problems, FGLS estimation of the Parks model, along with a number of its variants, has remained relevant. As noted above, the Parks model provides the underlying statistical foundation for Stata's *xtgls* command, and related estimators are available in Eviews. BK's Panel-Corrected Standard Error (PCSE) procedure is a modification of the full GLS-Parks estimator that preserves weighting of observations for autocorrelation, but uses a sandwich estimator to incorporate cross-sectional dependence when calculating standard errors. It is available in Stata as the *xtpcse* command. The PCSE estimator has proven very popular, as evidenced by over 1700 citations on Web of Science.

It is in this context that Reed and Ye (2011), henceforth RY, conducted Monte Carlo experiments to test a large number of OLS and FGLS-type panel data estimators, including as a subset the estimators studied by BK. They studied panel datasets for which the number of cross-sectional units (N) and time periods (T) were small to moderate in size. Cross-sectional units ranged in size from 5 to 77; and time periods ranged from 5 to 25. RY presented three recommendations to guide researchers facing the decision of which panel data estimator to use.

In their conclusion, RY called for additional experiments to confirm their recommendations. This paper responds to that call. We do so for four reasons. First, RY strive for external validity in their experiments because parameter values used in their Monte Carlo experiments were taken from actual panel datasets. In the Parks-type error structures used by BK and RY, there are often more than a thousand unique elements in the respective EVCN. Rather than attempting to set “plausible” values for all these parameters, RY estimate these from actual datasets, and then set these estimated values as population values for the subsequent experiments. However, because RY’s experiments were based on a relatively small number of datasets, there is concern that their recommendations may not apply to other datasets. A replication of RY with different datasets provides an opportunity to test the validity of their recommendations.

The second reason for following up RY is that it focuses on standard, “workhorse”, panel data estimators that are built into Stata and Eviews. Many researchers rely on the “built-in” panel data estimators that come with standard statistical packages. Knowing which ones of these are “best” in given situations is useful for these researchers.

A third reason for focussing on RY is that their study has a very practical ambition: to map observable characteristics of the data to a specific estimator choice. The superior performance of many estimators is often based on unobservable characteristics. For example, instrumental variable (IV) estimators are generally superior to OLS given a sufficient degree of endogeneity. In the absence of endogeneity, OLS will be superior because it is more efficient. But the degree of endogeneity is unobserved. Tests for endogeneity can provide some guidance, but they do not allow one to conclude that IV is necessarily better/more efficient than OLS in a given situation.¹ The ability to map data characteristics to estimator

¹ So, for example, tests and measures such as are found in Stock and Yogo (2005) and Baum et al. (2015) can identify the degree of bias in estimates, but they do not allow one to determine whether IV is more efficient than OLS.

selection is thus potentially very valuable for applied researchers. This supports further investigation of RY's recommendations.

The last reason for returning to RY is that there is a mistake in the design of their experiments. In attempting to construct explanatory variables that have the properties of "real world" data, they introduced additional autocorrelation that was not present in the source datasets. As autocorrelation in the explanatory variables exacerbates the effect of autocorrelation in the error term, this should affect their analysis. In fact, when we correct this error in their experimental design, we find that a modification of RY's three recommendations results in a virtually complete set of recommendations, identifying a "best" estimator for every data situation.

Our study proceeds as follows. Section 2 summarizes the experimental design and datasets used for our experiments. Section 3 presents the experimental findings. Section 4 concludes.

2. Experimental Design

The data generating process (DGP). The experimental design for our analysis is taken from RY. Given N cross-sectional units and T time periods, we model the following DGP,

$$(1) \quad \mathbf{y} = \mathbf{i}\beta_0 + \mathbf{x}\beta_x + \boldsymbol{\varepsilon},$$

where $\mathbf{y}$, $\mathbf{i}$, $\mathbf{x}$, are each $(NT \times 1)$ vectors, β_0 and β_x are scalars, and $\boldsymbol{\varepsilon}$ is an $(NT \times 1)$ vector of error terms such that

$$(2) \quad \boldsymbol{\varepsilon} \sim N(\mathbf{0}, \boldsymbol{\Omega}_{NT}),$$

where

$$(3) \quad \boldsymbol{\Omega}_{NT} = \boldsymbol{\Sigma} \otimes \boldsymbol{\Pi},$$

$$(4) \quad \boldsymbol{\Sigma} = \begin{bmatrix} \sigma_{\varepsilon,11} & \sigma_{\varepsilon,12} & \cdots & \sigma_{\varepsilon,1N} \\ \sigma_{\varepsilon,21} & \sigma_{\varepsilon,22} & \cdots & \sigma_{\varepsilon,2N} \\ \vdots & \vdots & \ddots & \vdots \\ \sigma_{\varepsilon,N1} & \sigma_{\varepsilon,N2} & \cdots & \sigma_{\varepsilon,NN} \end{bmatrix}, \text{ and}$$

$$(5) \quad \mathbf{\Pi} = \begin{bmatrix} 1 & \rho & \rho^2 & \cdots & \rho^{T-1} \\ \rho & 1 & \rho & \cdots & \rho^{T-2} \\ \rho^2 & \rho & 1 & \cdots & \rho^{T-3} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \rho^{T-1} & \rho^{T-2} & \rho^{T-3} & \cdots & 1 \end{bmatrix}^2.$$

$\mathbf{\Omega}_{NT}$ incorporates groupwise heteroskedasticity, time-invariant cross-sectional dependence, and first-order, common autocorrelation. To get realistic values for the respective EVCM elements, $\sigma_{\varepsilon,ij}$ and ρ , we estimate these parameters from actual datasets, using the same procedures that Stata and Eviews use in calculating their respective FGLS estimators.

Creation of simulated panel datasets. TABLE 1 lists the datasets that were employed in obtaining population parameter values for the DGPs in the Monte Carlo experiments. In order to evaluate the recommendations provided by RY, albeit with a corrected experimental design, we start with the same datasets they used. These are listed in the top panel of TABLE 1. However, we also use additional datasets that were not considered by RY. These are listed in the bottom panel of TABLE 1 (“new datasets”).

The first set of experiments draw data from the Penn World Table. For a given sized panel dataset, say $N=5$ and $T=5$, we take the first N cross-sectional units and regress the log of real GDP on the ratio of government expenditures to GDP and a set of country fixed effects for the first T available time periods. We save the residuals from that regression. We then use those residuals to obtain estimates of the individual elements of the EVCM, $\hat{\sigma}_{\varepsilon,ij}$, $i, j = 1, 2, \dots, N$, and $\hat{\rho}$. We then repeat that procedure for all possible samples of T contiguous years. These estimates are then averaged to obtain a “representative” EVCM,

² Following BK and RY, we set the AR(1), autocorrelation parameter, ρ , to be the same for all cross-sectional units.

$$(3') \quad \bar{\bar{\Omega}}_{NT} = \begin{bmatrix} \bar{\hat{\sigma}}_{\varepsilon,11} & \bar{\hat{\sigma}}_{\varepsilon,12} & \cdots & \bar{\hat{\sigma}}_{\varepsilon,1N} \\ \bar{\hat{\sigma}}_{\varepsilon,21} & \bar{\hat{\sigma}}_{\varepsilon,22} & \cdots & \bar{\hat{\sigma}}_{\varepsilon,2N} \\ \vdots & \vdots & \ddots & \vdots \\ \bar{\hat{\sigma}}_{\varepsilon,N1} & \bar{\hat{\sigma}}_{\varepsilon,N2} & \cdots & \bar{\hat{\sigma}}_{\varepsilon,NN} \end{bmatrix} \otimes \begin{bmatrix} 1 & \bar{\hat{\rho}} & \bar{\hat{\rho}}^2 & \cdots & \bar{\hat{\rho}}^{T-1} \\ \bar{\hat{\rho}} & 1 & \bar{\hat{\rho}} & \cdots & \bar{\hat{\rho}}^{T-2} \\ \bar{\hat{\rho}}^2 & \bar{\hat{\rho}} & 1 & \cdots & \bar{\hat{\rho}}^{T-3} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ \bar{\hat{\rho}}^{T-1} & \bar{\hat{\rho}}^{T-2} & \bar{\hat{\rho}}^{T-3} & \cdots & 1 \end{bmatrix}.$$

To obtain a representative vector of $\mathbf{x}$ values, we randomly select one contiguous, T -year period.³ Let these values be given by $\tilde{\mathbf{x}}$. Then for given values of β_0 and β_x , we generate simulated $\tilde{\mathbf{y}}$ values from the following DGP:

$$(6) \quad \tilde{\mathbf{y}} = \mathbf{i}\beta_0 + \tilde{\mathbf{x}}\beta_x + \tilde{\boldsymbol{\varepsilon}},$$

where $\tilde{\boldsymbol{\varepsilon}}$ consists of simulated, normally distributed error terms having mean 0 and an EVCM equal to $\bar{\bar{\Omega}}_{NT}$. The vector of $\tilde{\mathbf{y}}$ and $\tilde{\mathbf{x}}$ values are then used to obtain estimates of β_x for each of the estimators under study.

This procedure was followed for each of the N and T values listed in TABLE 1, and each of the respective datasets.⁴ Note that each N and T pair produces a unique set of $\hat{\sigma}_{\varepsilon,ij}$, $i, j = 1, 2, \dots, N$, and $\hat{\rho}$ values (and thus unique EVCM), as well as unique $\tilde{\mathbf{x}}$ values. Accordingly, each of the original sixteen datasets becomes the parent for anywhere from 15 to 25 artificial

³ RY made a mistake in their experimental design by averaging the $\mathbf{X}$ values. This introduced excessive autocorrelation in $\tilde{\mathbf{x}}$. When the error terms are serially correlated, the serial correlation in the regressor affects the variance of its OLS coefficient estimator variance. The following relationship connects the variance of OLS slope estimator characterised by first order serial correlation of both the error term and the regressor, $Var(\hat{\beta}_{AR(1)})$, on the one hand, and that of the usual OLS slope estimator, $Var(\hat{\beta}_{OLS})$, on the other (see Gujarati 2004, p 452): $Var(\hat{\beta}_{AR(1)}) = Var(\hat{\beta}_{OLS}) \left(\frac{1+r\rho}{1-r\rho} \right)$, where r and ρ denote the first order serial correlation coefficients of the regressor and the error term respectively. Thus, exaggerating the serial correlation in the regressor worsens the bias in the estimated coefficient standard error. We note that Beck and Katz (1995) made a related error on the other side in their Monte Carlo experiments by generating x_{it} values that were “random draws from a zero-mean normal distribution” (BK, page 638). By ignoring the role of autocorrelation in the explanatory variable, they diminished the problems caused by autocorrelation. This was pointed out in a replication study by Reed and Webb (2010).

⁴ The maximum N and T values listed in TABLE 1 are often less than the size of the panel dataset in the original dataset. For example, the original Dataset 1 used by RY contained data on 97 countries for 40 years (1961-2000). However, data issues, usually caused by problems with the Cholesky decomposition function in creating simulated error terms, forced us to limit the sizes of some of the panel datasets. For the same reason, the actual number of datasets we were able to create is less than the total possible combinations from pairing all possible N and T values in the table.

datasets, depending on the number of possible (N, T) combinations. These “offspring” datasets, besides having different sizes, also have different characteristics. For example, a cross-country dataset that has level of income as its dependent variable and that includes the world’s largest economies such as the US, China, Germany, Japan, and the UK, will have very different heteroskedasticity characteristics than a dataset that omits these countries. Further, cross-country dependencies will vary greatly depending on the specific countries that are included.

The datasets listed in TABLE 1 are quite diverse. In particular, the new datasets listed in the bottom panel are distinctly different from the original RY datasets. The original RY datasets used dependent variables that were income-based, either cross-country/GDP values (level and growth) or US state/PCPI values (level and growth). In contrast, the dependent variables for the new datasets are (i) international aid (Datasets 9 and 13), (ii) a democracy index (Datasets 10 and 14); (iii) crime per capita (Datasets 11 and 15), and (iv) a binary variable indicating conflict (Datasets 12 and 16). And not just the dependent variables, but the explanatory variables are very different. This should produce a wide variety of artificial panel datasets having very different EVCMS.

Sample characteristics of simulated datasets. TABLE 2 gives more detail regarding the datasets. Reported are measures of heteroskedasticity, autocorrelation, and cross-sectional dependence. These measures are calculated from the estimated elements of $\widehat{\Omega}_{NT}$. As before, the top panel reports details about the original RY datasets, while the new datasets are featured in the bottom panel. Within each panel, datasets are divided depending on whether $T \geq N$ or $T < N$. Each dataset produces either ten or eleven observations of $\hat{\beta}_x$, one for each estimator (more on the estimators below). There are fewer observations per dataset when $T < N$, because, as noted above, one of the estimators (the fully specified FGLS with heteroskedasticity, autocorrelation, and cross-sectional dependence; also known as the Parks estimator), cannot be estimated in this case.

Heteroskedasticity is calculated from a given dataset's group-specific variances. We sort the associated standard deviations and take the ratio of the 3rd and 1st quartile values,

$$\left(\frac{\sqrt{\hat{\sigma}_{\varepsilon, 3rd \text{ quartile}}}}{\sqrt{\hat{\sigma}_{\varepsilon, 1st \text{ quartile}}}} \right)^5 \quad \text{Larger values indicate greater heteroskedasticity. Autocorrelation is}$$

estimated by $\bar{\rho}$. These values should range between -1 and 1, with the expectation that most of the AR(1) parameters will be positive. Cross-sectional dependence is measured by the absolute values of the cross-sectional correlations, averaged over all possible pairs of cross-sectional units. These, in turn, are calculated from the respective cross-sectional covariances, $\hat{\sigma}_{\varepsilon, ij}$, $i, j = 1, 2, \dots, N$, $i \neq j$. These values should also range between 0 and 1.

Both the original RY datasets and the datasets new for this study demonstrate a wide range of error behaviours. Heteroskedasticity ranges from a low of 1.21 to a high of 40.21.⁶ Autocorrelation ranges from -0.06 to 0.79, and cross-sectional correlation from 0.20 to 0.79. The new datasets are generally characterized by greater heteroskedasticity and cross-sectional dependence, but lesser autocorrelation.

The estimators. Through this gauntlet of diverse data environments we run the respective estimators. These are identified in TABLE 3. These are the same estimators studied by RY. All of the estimators correspond to a particular Stata or Eviews panel data estimator.⁷ Each estimator is a special case of the following:

$$(7) \quad \hat{\beta} = (X'W^{-1}X)^{-1}X'W^{-1}y$$

$$(8) \quad Var(\hat{\beta}) = (X'W^{-1}X)^{-1}X'W^{-1}\hat{\Omega}W^{-1}X(X'W^{-1}X)^{-1}$$

⁵ Note that the $\hat{\sigma}_{\varepsilon}$ terms are variances, and not standard deviations.

⁶ The particularly high heteroskedasticity values come from Datasets 12 and 16, where the dependent variable is zero-one.

⁷ The Appendix lists the specific commands in Stata or Eviews that correspond to each estimator.

where $\mathbf{X} = [\mathbf{i} \ \tilde{\mathbf{x}}]$, $\hat{\boldsymbol{\beta}} = [\hat{\beta}_0 \ \hat{\beta}_x]$, $\mathbf{W}$ is the “weighting” matrix, and $\hat{\boldsymbol{\Omega}}$ is the estimated EVCM.⁸ For example, in the case of OLS with an assumed IID error structure (Estimator 1), $\mathbf{W} = \mathbf{I}$ and $\hat{\boldsymbol{\Omega}} = \hat{\sigma}^2 \mathbf{I}$. In the case of Estimator 5 (FGLS-1A), $\mathbf{W} = \hat{\boldsymbol{\Omega}}$, where $\hat{\boldsymbol{\Omega}}$ is the diagonal matrix with group-specific variances on the main diagonal. Estimator 9 (FGLS-1B) has the same weighting matrix $\mathbf{W}$, and thus produces an identical estimate, $\hat{\boldsymbol{\beta}}$, but estimates $\boldsymbol{\Omega}$ using a robust estimator that clusters on time period, and thus produces different standard errors than Estimator 5.

TABLE 3 employs the notation that estimators with the same weighting matrix $\mathbf{W}$ have the same number index. Estimators with different $\hat{\boldsymbol{\Omega}}$ matrices have different letter indices. So all the FGLS-1 estimators use the same weighting matrix (based on groupwise heteroskedasticity), but FGLS-1A calculates different standard errors than FGLS-1B, FGLS-1C, and FGLS-1D.

Estimators 1, 7, and 8 are particularly worth noting. Estimator 1 is conventional (pooled) OLS.⁹ This will serve as the benchmark estimator against which the other estimators will be compared. Estimator 7 is the Parks estimator. It is asymptotically efficient, but requires $T \geq N$.¹⁰ Estimator 8 is BK’s PCSE estimator which has become a popular substitute for the Parks estimator because of its claimed finite sample advantages.

Performance measures. The experiments compare the respective panel data estimators on two dimensions, efficiency and accuracy in hypothesis testing. An experiment consists of 1000 estimates derived from a 1000 panel data samples simulated from a DGP representing a

⁸ Note that $\hat{\boldsymbol{\Omega}} \neq \tilde{\boldsymbol{\Omega}}_{NT}$. $\tilde{\boldsymbol{\Omega}}_{NT}$ is the population EVCM used in the DGP to generate the simulated $\tilde{\mathbf{y}}$ and $\tilde{\mathbf{x}}$ data. $\hat{\boldsymbol{\Omega}}$ is the EVCM estimated from residuals generated by regressing $\tilde{\mathbf{y}}$ on $\tilde{\mathbf{x}}$.

⁹ Note that the DGP does not contain fixed effects, so we omit fixed effects estimators from the choice set.

¹⁰ It is possible to estimate the full Parks model in Stata when $T < N$. This is made possible through the use of a generalized inverse function in Stata that allows one to invert matrices that are not full rank. However, our own investigations indicate that the resulting estimators do not perform well.

given “offspring” dataset. For each experiment and each estimator, we calculate an *EFFICIENCY* value defined by,

$$(9) \quad EFFICIENCY_{Estimator} = 100 \cdot \frac{\sqrt{\sum_{r=1}^R (\hat{\beta}_{Estimator}^{(r)} - \beta_x)^2}}{\sqrt{\sum_{r=1}^R (\hat{\beta}_{OLS}^{(r)} - \beta_x)^2}},$$

where β_x is the true value of the slope coefficient, and $\hat{\beta}_{OLS}^{(r)}$ and $\hat{\beta}_{Estimator}^{(r)}$ are the estimated values of β_x in a given replication r as estimated by OLS and the estimator that is being compared to OLS, respectively. Smaller values indicate a more efficient estimator. OLS is defined to have an *EFFICIENCY* value of 100. Estimators with *EFFICIENCY* values less than 100 are thus more efficient than OLS for datasets having the given characteristics.

To measure accuracy in hypothesis testing, we calculate two measures. The first is the coverage rate, *Coverage*, defined as the percent of 95% confidence intervals around $\hat{\beta}_x$ that include the true value of β_x . We also calculate the absolute value of the difference between 95% and the coverage rate, $|95 - Coverage|$. Estimators for which $|95 - Coverage|$ is closest to zero are judged to be superior with respect to accuracy in hypothesis testing.

As seen in TABLE 3, estimators 5, 9, 10, and 11 all share the same weighting matrix, $\mathbf{W}$, weighting solely on (groupwise) heteroskedasticity. As a result, these estimators will produce identical coefficient estimates $\hat{\beta}$ when using the same data (cf. Equation 7). Thus, in comparing estimators on the dimension of efficiency, we treat these estimators as one and refer to Estimator 5/9/10/11. When it comes to assessing their accuracy in hypothesis testing, they will be treated separately because they produce different estimates of $Var(\hat{\beta})$ (cf. Equation 8).

RY’s three recommendations. Based on their analysis of the performances of the eleven estimators in TABLE 3, RY provide three recommendations.¹¹

1. When the primary concern is efficiency and $T/N \geq 1.50$, use *Estimator 7*.

¹¹ In order to make their recommendations easier to understand, we have replaced their terminology with the nomenclature from this paper. The substituted terms are italicized.

2. When the primary concern is efficiency, $T/N < 1$, and *Heteroskedasticity* > 1.67 , use either *Estimator 5* or *Estimator 6*.
3. When the primary concern is constructing accurate confidence intervals and *Autocorrelation* < 0.30 , use either *Estimator 8* or *Estimator 4*.

These recommendations are designed as guides for applied researchers, mapping observed/measurable characteristics of the data – such as the ratio of time periods to units, or the degree of heteroskedasticity or autocorrelation – to the choice of a “best” estimator.

Two things are noteworthy in this regard. First, the recommendations have “gaps.” For example, when choosing estimators on the basis of efficiency, there is a recommendation for cases where $T/N \geq 1.50$ and $T/N < 1$, but nothing for $1 \leq T/N < 1.50$. And when it comes to selecting an estimator based on accurate confidence intervals, and hence preferred for hypothesis testing, there is no recommendation when *Autocorrelation* ≥ 0.30 . The reason for these gaps is that RY could not identify a consistently best estimator for these data situations.

Also noteworthy is the fact that RY recommend different estimators depending on whether one’s primary interest is efficiency or accuracy in hypothesis testing. While this is unusual, it is not contradictory. The expression for $Var(\hat{\beta})$ in Equation (8) does not have finite sample validity. The substitution of $\hat{\Omega}$ for Ω is justified on the basis of the “analogy principle” (Manski, 1988). While correct asymptotically -- assuming the respective estimates of the EVCM elements are consistent -- it may be a better or worse substitute in finite samples for some estimators versus others depending on the specifics of the deviation between $\hat{\Omega}$ and Ω . Further, because $\hat{\Omega}$ factors differently into Equations (7) and (8), it is possible that this deviation affects an estimator’s relative performance in hypothesis testing more or less than its relative performance in efficiency.

To summarize, RY’s recommendations provide a potentially useful guide to applied researchers facing a choice of panel data estimators. However, their recommendations are incomplete, and they have the unusual feature of advising different estimators for coefficient

efficiency and accuracy in hypothesis testing. While their analysis introduced additional autocorrelation in the simulated values of the explanatory variables, it's not clear to what extent this affected their results. Our analysis attempts to see whether correcting this mistake alters their recommendations, and if it does, whether the new recommendations are robust when these recommendations are applied to entirely new datasets.

3. Results

Efficiency. This section compares the performance of the respective estimators. All the results follow the procedures discussed above, and incorporate the correction to RY's original experimental design.¹² TABLE 4 reports average performance measures for efficiency for different subgroups of experiments. The first two columns report average *EFFICIENCY* values for all experiments according to whether $T/N \leq 1.5$ or $T/N > 1.5$, where *EFFICIENCY* is calculated using Equation (9). We choose the cut-off of 1.5 to be consistent with RY's first recommendation, and also based on our own analysis. The next two columns provide a different perspective on efficiency. They report the percent of experiments where a given estimator is more efficient than OLS. The "best" estimators are indicated by yellow-highlighting the respective cells in the table.

The top panel reports the results for the datasets used by RY. According to RY's first recommendation, when researchers are primarily interested in efficiency and T/N is greater than 1.5, they should choose Estimator 7, the Parks estimator. Our findings confirm this recommendation for the Reed and Ye (2011) datasets. When $T/N > 1.5$, the average *EFFICIENCY* of Estimator 7 is 45.5, substantially lower than that of the other estimators. Moreover, Estimator 7 is always better than OLS (100 percent). The other estimators are more efficient than OLS most, but not all, of the time.

¹² While we do not report the results here, we confirm that we were able to reproduce all of RY's results when using their original experimental design.

The bottom part of the panel reports the results of experiments based on the new datasets. This represents a clean “out of sample” test of RY’s recommendation, because none of these datasets were included in RY’s analysis. Focussing again on the experiments where $T/N > 1.5$, we see that Estimator 7 has a much lower average *EFFICIENCY* value than the other estimators. Further, it is more efficient than OLS approximately 98 percent of the time, tied for best most among all estimators.

Averages can mask much variation. Accordingly, FIGURES 1 and 2 plot the average *EFFICIENCY* values for each of the estimators as a function of T/N when $T/N > 1.5$. FIGURE 1 does this for the RY datasets, and FIGURE 2 does this for the new datasets. The dotted, black line at Average Efficiency = 100 represents the OLS estimator, which serves as a benchmark for the other estimators.

Each line connects a series of points that report average *EFFICIENCY*, where the lines have been smoothed for the sake of readability. There are five points underlying each line in FIGURE 1 (for $T/N = 2.0, 2.5, 3.0, 4.0$ and 5.0), and seven points in FIGURE 2 ($T/N = 1.9, 2.0, 2.5, 3.0, 3.8, 4.0$ and 5.0). The reason the lines do not change monotonically with T/N is that other characteristics (heteroskedasticity, autocorrelation, cross-sectional dependence) are changing simultaneously with T/N . The movement from one T/N value to another is, in fact, a movement to a different DGP, with different population EVCM values.

Each of the estimators are color-coded in FIGURES 1 and 2. It is clear from both figures that the light blue line, corresponding to Estimator 7 (the Parks estimator), strictly dominates the others. For every T/N value included in our analysis, the average *EFFICIENCY* value for this estimator lies strictly below that of the other estimators, indicating greater efficiency. This confirms RY’s first recommendation.

We return to TABLE 4 and next examine the experiments where $T/N \leq 1.5$. While Estimator 7 is included in the table, its results are not directly comparable to the other

estimators because its results are based on a much smaller number of experiments, since it cannot be estimated when $T/N < 1.0$. Ignoring Estimator 7 for the moment, it is seen that Estimator 6 performs better than the other estimators both in terms of having a lower average *EFFICIENCY* value (74.7 and 48.0 for the RY and new datasets, respectively), and in terms of besting OLS more frequently than the other estimators (89.1 and 99.0 percent, respectively). Estimator 6 is essentially the Parks estimator (Estimator 7), except that it does not accommodate cross-sectional dependence.

FIGURES 3 and 4 further highlight the superior performance of Estimator 6 when it comes to efficiency. We first note that the lines in the figures connect a larger number of points than in the preceding figures. There are 16 points underlying each line in FIGURE 3 (for $T/N = 0.13, 0.19, 0.20, 0.21, 0.26, 0.30, 0.31, 0.32, 0.40, 0.42, 0.50, 0.52, 0.75, 1.00, 1.25$, and 1.50), and 15 points in FIGURE 4 ($T/N = 0.13, 0.19, 0.20, 0.25, 0.26, 0.30, 0.32, 0.38, 0.40, 0.50, 0.75, 0.95, 1.00, 1.25$, and 1.50). Estimator 6 is represented by the solid black line.

With one exception, Estimator 6 strictly dominates the other estimators over all values of T/N reported in FIGURES 3 and 4. The lone exception involves Estimator 7 in the Reed and Ye (2011) datasets for $T/N = 1.50$. For smaller values of T/N (1.00 and 1.25), Estimator 6 lies strictly below Estimator 7 (indicating superior efficiency). When we turn to FIGURE 4 and the new datasets, we see that Estimator 6 bests Estimator 7 even when $T/N = 1.50$. Thus, our results indicate that $T/N = 1.50$ is a crossing-over point. For values less than that, Estimator 6 is most efficient. For values greater than that, Estimator 7 is most efficient. For values in the immediate vicinity of 1.50, either estimator may be most efficient, depending on other characteristics of the dataset.

It is interesting to note that the superior performance of Estimator 6 for $1.0 \leq T/N < 1.5$ is an example of the “shrinkage principle.” This principle “asserts that the imposition of restrictions -- even false restrictions” can improve estimator performance (Diebold, 2007, p.

45). Even though the population EVCM is characterized by cross-sectional dependence, the estimator that “falsely” omits cross-sectional dependence (Estimator 6) outperforms the estimator that correctly includes it (Estimator 7). The reason this “false restriction” is effective in these cases is because there are insufficient observations to obtain reliable estimates of the cross-sectional covariances in Σ (cf. Equation 3).

Our findings call for a modification of RY’s second recommendation, which states: “When the primary concern is efficiency, $T/N < 1$, and *Heteroskedasticity* > 1.67 , use either *Estimator 5* or *Estimator 6*.” For one, there is no need to condition the recommendation on heteroskedasticity. Second, Estimator 6 dominates Estimator 5 for all values of $T/N \leq 1.5$, so that Estimator 5 can be omitted as a “best” option. And lastly, the superior performance of Estimator 6 extends for a wider range of T/N values than determined by RY.

Taken together, the above results sketch a (virtually) complete decision tree for choosing the most efficient panel data estimator, provided the estimators the researcher is choosing from are included in Stata’s or Eviews’ standard statistical software package. This can be summarized in the following two modified recommendations:

RECOMMENDATION 1: When the primary concern is efficiency and $T/N > 1.50$, use Estimator 7.

RECOMMENDATION 2: When the primary concern is efficiency and $T/N < 1.50$, use Estimator 6.

Accuracy in hypothesis testing. TABLE 5 reports performance results with respect to accuracy in hypothesis testing. The key columns are those that report the average value of the absolute difference between 95 percent and the coverage rate, $|95 - Coverage|$. An estimator should have a coverage rate close to 95 percent. Coverage rates less than (greater than) than 95 percent will reject the null hypothesis $H_0: \beta_x = its\ true\ value$ too often (not often enough). Both outcomes distort hypothesis testing. Thus the “best” estimator on the dimension of accuracy in hypothesis testing is one for which $|95 - Coverage|$ is closest to zero.

The table has four panels. The first two panels report performance results for the experiments where $T/N \geq 1$ for the Reed and Ye (2011) datasets and the new datasets, respectively. The next two panels report results for $T/N < 1$. $T/N = 1$ is selected as the cut-off because Estimator 7 (the Parks estimator) cannot be estimated when T/N is less than this.

The table also has four columns, with the first two columns collecting experiments where the associated datasets are characterized by *Autocorrelation* values less than 0.30, and the next two columns reporting results when *Autocorrelation* ≥ 0.30 . This cut-off is motivated by RY's third recommendation. RY found that Estimator 8 (the PCSE estimator) performed best for hypothesis testing when *Autocorrelation* < 0.30 , while no estimator performed acceptably for autocorrelation values larger than this.

In the table, cells where Estimator 8 has the smallest $|95 - \text{Coverage}|$ values are color-coded yellow. Cells where Estimator 8 has the second smallest $|95 - \text{Coverage}|$ value are color-coded green. An inspection of the first two columns confirms RY's third recommendation for both the Reed and Ye (2011) datasets and the new datasets, irrespective of the value of T/N . Across the four subsets of experiments (Reed and Ye, 2011, $T/N < 1$ and $T/N \geq 1$; and New Datasets, $T/N < 1$ and $T/N \geq 1$), the values of $|95 - \text{Coverage}|$ range from a low of 3.5 to a high of 5.5.

However, the results allow one to go even further. When *Autocorrelation* ≥ 0.30 , Estimator 8 either has the smallest, or close to the smallest $|95 - \text{Coverage}|$ value in each of the four subsamples. Further, the corresponding values of $|95 - \text{Coverage}|$ are quite small, ranging from 1.8 to 3.3.

FIGURES 5 to 8 provide more detail about the relative performances of the estimators with respect to hypothesis testing. Unlike the previous tables, there are a great many unique points on the horizontal axis, which causes the lines to be far less regular. For example, each estimator line in FIGURE 5 connects 80 individual points. And because each estimator has a

unique estimate of the estimated coefficient's standard error, there are now either 11 lines (FIGURES 5 and 7) or 10 (FIGURES 6 and 8), to include in each figure.

In order to maintain readability, FIGURES 5 and 6 highlight just three estimators: Estimator 8 (solid black line), Estimator 6 (solid red line), and Estimator 7 (solid blue line). The other estimators are represented by identical dotted lines. We focus on Estimator 8 because TABLE 5 identified this estimator as “best” on the dimension of accuracy in hypothesis testing. We also highlight Estimator 6 because TABLE 5 indicates that this estimator also does relatively well. And we draw attention to Estimator 7 – the Parks estimator and the estimator chosen as best for efficiency when $T/N > 1.5$ – to show just how poorly this estimator performs when it comes to hypothesis testing. FIGURES 7 and 8 omit Estimator 7 because it cannot be estimated when $T/N < 1$.

FIGURES 5 and 6 illustrate the general point that hypothesis testing can be very unreliable when using standard panel data estimators. While the performance of Estimator 7 is uniquely dismal, many of the other estimators also perform unacceptably poorly. Even the “best” estimator, Estimator 8, has instances where its performance is less than stellar.

Looking across all four figures, it is clear that Estimator 8 generally dominates the other estimators across the diverse collection of experiments represented in FIGURES 5 through 8. While there are instances where one or more of the other estimators perform better than Estimator 8 in a given experiment, it is difficult to know whether this is anything more than sampling error. TABLE 5, along with FIGURES 5 through 8 allow then the following modification to RY's third recommendation:

RECOMMENDATION 3: When the primary concern is hypothesis testing, use Estimator 8.

Together, Recommendations 1 through 3 allow an applied researcher choosing panel data estimators from Stata or Eviews to easily select the “best” estimator. When it comes to choosing an estimator for efficiency, the researcher only need to know the size of the panel

dataset (N and T). That is sufficient to determine his/her selection. When it comes to choosing an estimator for hypothesis testing, the choice is even simpler: choose Estimator 8, the PCSE estimator.

Bootstrapping. While useful to applied researchers, the recommendations above require one to use different estimators depending on whether the primary interest is coefficient efficiency or accuracy in hypothesis testing. At the very least, this is awkward and difficult to motivate. It would be better if a researcher could use the same estimator for both estimation and inference.

In a recent paper, Mantobaye et al. (2016) develop bootstrap methods for SUR models with autocorrelated errors. In this section, we demonstrate the feasibility of these methods by bootstrapping the Parks estimator. TABLE 6 compares the accuracy of the PCSE estimator with the parametric bootstrap from Mantobaye et al. (2016). A full comparison lies beyond the purview of this study. However, the table provides some examples using Dataset 1 (cf. TABLE 1) for varying N and T values. In every case, the bootstrapped method produces more accurate inference results than the PCSE estimator. For example, when $N = 5$ and $T = 10$, 87.3 percent of the 95% confidence intervals calculated from the PCSE estimator contain the true value of β_x . In contrast, 95.2 percent of confidence intervals contain the true value of β_x using the bootstrapped method.

The advantage of bootstrapping is it allows one to use the same estimator for both estimation and inference, without the need of using an entirely different estimator for hypothesis testing. The disadvantage is that these methods are not yet readily available in statistical software packages, making implementation difficult and time-consuming.

4. Conclusion

This study uses Monte Carlo experiments to produce new evidence on the performance of a wide range of panel data estimators. It focuses on estimators that are readily available in

statistical software packages such as Stata and Eviews, and for which the number of cross-sectional units (N) and time periods (T) are small to moderate in size. It identifies two estimators, a FGLS estimator that weights on heteroskedasticity and the Parks estimator, as being most efficient depending on whether T/N is less than or greater than 1.50, respectively. And it identifies the PCSE estimator as being best for hypothesis testing.

While it is true that the use of different estimators for estimation and inference is unusual and may be difficult to motivate, it has the advantage of using easily available estimators to produce the best results on both dimensions. Bootstrapping provides a promising alternative, but programs to implement these methods are not yet readily available.

We note that while OLS with cluster robust standard errors is widely used by applied researchers, our experiments find that it performs relatively poorly on both efficiency and inference grounds for the small to moderately-sized panel datasets studied here. Thus, another contribution of our study is that it alerts researchers that there are better alternatives to OLS when the underlying DGP is assumed to be of the Parks variety.

Our analysis leaves several issues unresolved. One such issue is unbalanced data. All of the experiments above assumed that the panel datasets are balanced. It is not clear how these recommendations need to be modified when this is not the case. Another issue concerns dynamic panel data. All of the experiments above assumed static DGPs. As is well known, dynamic panel data have a number of complications that require special attention. Similarly, our analysis does not include many other panel data estimators, some of which we mention in the introduction above.

While we acknowledge the limitations of our study, it is still the case that the panel data estimators that come packaged in Stata and Eviews are widely used by many researchers. The fact that the best estimators separate out so clearly, across a wide variety of data environments,

is striking. While additional work needs to be done, the findings of this study provide a useful start for researchers deciding which panel data estimator they should use.

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TABLE 1
Description of Datasets Used to Generate Population Parameters

<i>Dataset</i>	<i>Source</i>	<i>Dependent Variable</i>	<i>Independent Variables</i>	<i>N</i>	<i>T</i>
<i>REED AND YE (2011) DATASETS</i>					
1	Penn World Table	Log of real GDP	Ratio of government expenditures to GDP Country fixed effects	5, 10, 20, 50, 77	5, 10, 15, 20, 25
2	Penn World Table	Real GDP growth	Ratio of government expenditures to GDP Country fixed effects	5, 10, 20, 50, 77	5, 10, 15, 20, 25
3	Reed (2008)	Log of real state PCPI	Tax Burden State fixed effects	5, 10, 20, 48	5, 10, 15, 20, 25
4	Reed (2008)	Real state PCPI growth	Tax Burden State fixed effects	5, 10, 20, 48	5, 10, 15, 20, 25
5	Penn World Table	Log of real GDP	Ratio of government expenditures to GDP Country fixed effects Time fixed effects	5, 10, 20, 50, 77	5, 10, 15, 20, 25
6	Penn World Table	Real GDP growth	Ratio of government expenditures to GDP Country fixed effects Time fixed effects	5, 10, 20, 50, 77	5, 10, 15, 20, 25
7	Reed (2008)	Log of real state PCPI	Tax Burden State fixed effects Time fixed effects	5, 10, 20, 48	5, 10, 15, 20, 25
8	Reed (2008)	Real state PCPI growth	Tax Burden State fixed effects Time fixed effects	5, 10, 20, 48	5, 10, 15, 20, 25

<i>Dataset</i>	<i>Source</i>	<i>Dependent Variable</i>	<i>Independent Variables</i>	<i>N</i>	<i>T</i>
NEW DATASETS					
9	Kersting & Kilby (2014)	Gross Aid Disbursement as Share of GDP (Germany Aid Allocation)	Freedom House Score Country fixed effects	5, 10, 20, 50, 77	10, 15, 20, 25
10	Casper & Tufis (2003)	Vanhanen's Democracy Index	Primary education enrolment (share of population) Country fixed effects	5, 10, 20, 50	10, 15, 20, 25
11	Biagi et al. (2012)	Crime per 100000 inhabitants	Tourists arrivals per square kilometre Country fixed effects	5, 10, 20, 50, 77	10, 15, 19
12	Nunn & Qian (2014)	Any Conflict	US-Wheat Aid (1000 MT) Country fixed effects	5, 10, 20, 50, 77	10, 15, 20, 25
13	Kersting & Kilby (2014)	Gross Aid Disbursement as Share of GDP (Germany Aid Allocation)	Freedom House Score Country fixed effects Year fixed effects	5, 10, 20, 50, 77	10, 15, 20, 25
14	Casper & Tufis (2003)	Vanhanen's Democracy Index	Primary education enrolment (share of population) Country fixed effects Year fixed effects	5, 10, 20, 50	10, 15, 20, 25
15	Biagi et al. (2012)	Crime per 100000 inhabitants	Tourists arrivals per square kilometre Country fixed effects Year fixed effects	5, 10, 20, 50, 77	10, 15, 19
16	Nunn & Qian (2014)	Any Conflict	US-Wheat Aid (1000 MT) Country fixed effects Year fixed effects	5, 10, 20, 50, 77	10, 15, 20, 25

TABLE 2
Description of Simulated Datasets Used in the Experiments

		<i>Heteroskedasticity</i>	<i>Autocorrelation</i>	<i>Cross-sectional Dependence</i>
<i>REED AND YE (2011) DATASETS</i>				
<i>N ≤ T</i> <i>(80 datasets;</i> <i>880 observations)</i>	<i>Minimum</i>	1.21	-0.06	0.20
	<i>Mean</i>	1.68	0.36	0.44
	<i>Maximum</i>	2.35	0.78	0.90
<i>N > T</i> <i>(64 datasets;</i> <i>640 observations)</i>	<i>Minimum</i>	1.34	-0.04	0.22
	<i>Mean</i>	1.76	0.34	0.43
	<i>Maximum</i>	2.25	0.79	0.79
<i>NEW DATASETS</i>				
<i>N ≤ T</i> <i>(72 datasets;</i> <i>792 observations)</i>	<i>Minimum</i>	1.26	0.08	0.22
	<i>Mean</i>	4.47	0.47	0.35
	<i>Maximum</i>	40.21	0.73	0.52
<i>N > T</i> <i>(68 datasets;</i> <i>680 observations)</i>	<i>Minimum</i>	1.47	0.16	0.23
	<i>Mean</i>	6.93	0.46	0.34
	<i>Maximum</i>	34.91	0.73	0.49

NOTE: For more details on the construction of the simulated datasets, see Section 2 in the text.

TABLE 3
List and Description of Panel Data Estimators to Be Studied

<i>Estimator</i>	<i>Procedure</i>	<i>Assumed Error Structure</i>
1	OLS-1A	IID
2	OLS-1B	Robust heteroskedasticity
3	OLS-1C	Robust heteroskedasticity + Robust autocorrelation
4	OLS-1D	Robust heteroskedasticity + Robust cross-sectional dependence
5	FGLS-1A	Groupwise heteroskedasticity
6	FGLS-2	Groupwise heteroskedasticity + autocorrelation
7	FGLS-3 (Parks)	Groupwise heteroskedasticity + autocorrelation + cross-sectional dependence
8	FGLS-4 (PCSE)	Groupwise heteroskedasticity + autocorrelation + cross-sectional dependence
9	FGLS-1B	Weight = Groupwise heteroskedasticity Var-Cov = Robust heteroskedasticity + Robust cross-sectional dependence
10	FGLS-1C	Weight = Groupwise heteroscedasticity Var-Cov = Robust heteroskedasticity + Robust autocorrelation
11	FGLS-1D	Weight = Groupwise heteroskedasticity Var-Cov = Robust heteroskedasticity

NOTE: Interpretation of the numbering and lettering of the procedures is given in Section 2 in the text. Further details about the estimator is given in the Appendix.

TABLE 4
Comparison of Estimator *EFFICIENCY*

<i>Estimator</i>	<i>Average EFFICIENCY</i>		<i>Percentage of Times the Estimator Is More Efficient Than OLS</i>	
	<i>T/N > 1.5</i> (1)	<i>T/N ≤ 1.5</i> (2)	<i>T/N > 1.5</i> (3)	<i>T/N ≤ 1.5</i> (4)
<i>REED AND YE (2011) DATASETS</i>				
<i>Estimator 5/9/10/11</i>	96.6	84.2	68.8	78.9
<i>Estimator 6</i>	82.8	74.7	75.0	89.1
<i>Estimator 7</i>	45.5	66.1*	100.0	100.0*
<i>Estimator 8</i>	86.9	89.1	62.5	72.7
<i>NEW DATASETS</i>				
<i>Estimator 5/9/10/11</i>	70.8	54.5	88.6	97.9
<i>Estimator 6</i>	61.5	48.0	97.7	99.0
<i>Estimator 7</i>	46.9	80.1*	97.7	96.4*
<i>Estimator 8</i>	85.1	92.1	95.5	80.2

* The results for Estimator 7 are not comparable to the other estimators when $T/N \leq 1.5$ because they are based on a subset of the experiments, since Estimator 7 cannot be estimated when $T/N < 1.0$.

NOTE: The *EFFICIENCY* measure is defined in Section 2 in the text. Yellow-coloured cells indicate “best” estimator for a given data-type.

TABLE 5
Comparison of Estimator Coverage Rates

	<i>Autocorrelation</i> < 0.30		<i>Autocorrelation</i> ≥ 0.30	
	<i>Coverage</i> (1)	<i> 95 – Coverage </i> (2)	<i>Coverage</i> (3)	<i> 95 – Coverage </i> (4)
<i>REED AND YE (2011) DATASETS (T/N ≥ 1)</i>				
<i>Estimator 1</i>	65.7	29.3	90.9	6.1
<i>Estimator 2</i>	64.1	30.9	91.0	4.9
<i>Estimator 3</i>	86.5	8.9	88.6	6.5
<i>Estimator 4</i>	60.1	34.9	91.5	3.8
<i>Estimator 5</i>	59.8	35.2	88.6	6.4
<i>Estimator 6</i>	88.0	7.1	90.9	4.4
<i>Estimator 7</i>	42.9	52.1	45.6	49.4
<i>Estimator 8</i>	89.5	5.5	92.7	2.3
<i>Estimator 9</i>	51.9	43.1	85.6	9.4
<i>Estimator 10</i>	70.5	24.5	77.3	17.7
<i>Estimator 11</i>	58.5	36.5	88.2	6.8
<i>NEW DATASETS (T/N ≥ 1)</i>				
<i>Estimator 1</i>	87.9	9.3	74.6	21.4
<i>Estimator 2</i>	83.1	11.9	73.2	22.0
<i>Estimator 3</i>	88.4	6.6	90.2	6.7
<i>Estimator 4</i>	83.6	11.4	74.7	20.3
<i>Estimator 5</i>	85.8	9.2	73.4	22.9
<i>Estimator 6</i>	90.9	4.1	90.9	5.7
<i>Estimator 7</i>	38.1	56.9	42.0	53.0
<i>Estimator 8</i>	91.4	3.6	92.1	3.3
<i>Estimator 9</i>	75.5	19.5	64.7	30.3
<i>Estimator 10</i>	68.9	26.1	72.7	22.4
<i>Estimator 11</i>	80.6	14.4	68.6	26.4

	<i>Autocorrelation</i> < 0.30		<i>Autocorrelation</i> ≥ 0.30	
	<i>Coverage</i> (1)	<i> 95 – Coverage </i> (2)	<i>Coverage</i> (3)	<i> 95 – Coverage </i> (4)
REED AND YE (2011) DATASETS (<i>T/N</i> < 1)				
<i>Estimator 1</i>	70.4	24.6	93.8	5.8
<i>Estimator 2</i>	67.1	27.9	93.7	4.0
<i>Estimator 3</i>	91.7	5.3	92.4	4.8
<i>Estimator 4</i>	61.9	33.1	94.1	1.3
<i>Estimator 5</i>	60.3	34.7	92.6	3.7
<i>Estimator 6</i>	86.9	8.2	93.2	3.4
<i>Estimator 7</i>	---	---	---	---
<i>Estimator 8</i>	90.6	4.4	93.3	1.8
<i>Estimator 9</i>	50.3	44.7	87.2	7.8
<i>Estimator 10</i>	76.6	18.4	86.2	8.8
<i>Estimator 11</i>	59.2	35.8	92.2	3.8
NEW DATASETS (<i>T/N</i> < 1)				
<i>Estimator 1</i>	84.0	11.2	80.2	15.2
<i>Estimator 2</i>	81.9	13.1	78.2	16.8
<i>Estimator 3</i>	83.5	11.5	93.6	3.3
<i>Estimator 4</i>	88.3	6.7	75.6	19.4
<i>Estimator 5</i>	88.3	8.0	75.8	20.5
<i>Estimator 6</i>	93.6	4.0	93.2	3.9
<i>Estimator 7</i>	---	---	---	---
<i>Estimator 8</i>	91.5	3.5	92.3	2.7
<i>Estimator 9</i>	71.8	23.2	63.6	31.4
<i>Estimator 10</i>	82.7	12.3	82.9	12.1
<i>Estimator 11</i>	84.4	10.6	71.2	23.8

NOTE The performance measures *Coverage* and *|95 – Coverage|* are defined in Section 2 in the text. A yellow-coloured cell indicates that Estimator 8 performs best for a given data-type. A green-coloured cell indicates that this estimator is second best.

TABLE 6
A Comparison of the PCSE and Bootstrapped Parks Estimators
With Respect to Inference: An Example

<i>N</i>	<i>T</i>	<i>PCSE</i>		<i>Estimator 7 - Bootstrapped</i>	
		<i>Coverage</i> <i>(1)</i>	<i> 95 – Coverage </i> <i>(2)</i>	<i>Coverage</i> <i>(3)</i>	<i> 95 – Coverage </i> <i>(4)</i>
<i>5</i>	<i>10</i>	87.3	7.7	95.2	0.2
<i>5</i>	<i>15</i>	89.8	5.2	95.4	0.4
<i>5</i>	<i>20</i>	90.0	5.0	95.2	0.2
<i>5</i>	<i>25</i>	92.5	2.5	96.4	1.4
<i>10</i>	<i>10</i>	88.3	6.7	97.3	2.3
<i>10</i>	<i>15</i>	91.0	4.0	98.5	3.5
<i>10</i>	<i>20</i>	92.5	2.5	96.4	1.4
<i>10</i>	<i>25</i>	93.0	2.0	96.3	1.3

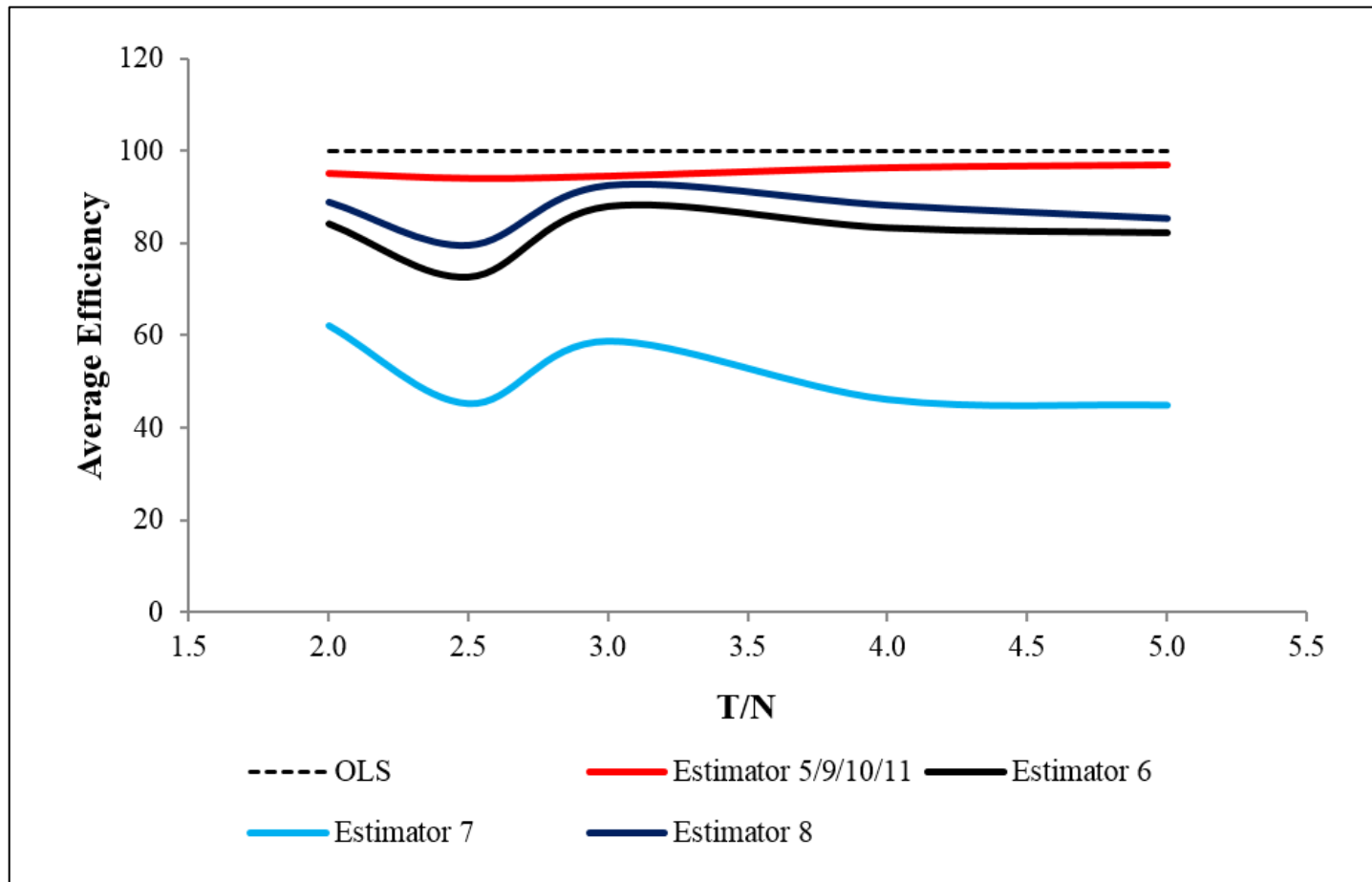
NOTE: PCSE coverage rates are taken from Monte Carlo experiments using Dataset 1 and the respective *N* and *T* values. Bootstrapped coverage rates are calculated using the parametric bootstrap method of Mantobaye et al. (2016).

APPENDIX
List and Description of Panel Data Estimators

<i>Estimator</i>	<i>Package</i>	<i>Command</i>
1	Stata	command = xtreg
2	Stata	command = xtreg options = robust
3	Stata	command = xtreg options = cluster (name of cross-sectional variable)
4	Stata	command = xtreg options = cluster (name of time period variable)
5	Stata	command = xtgls options = corr(independent) panels(heteroscedastic)
6	Stata	command = xtgls options = corr(ar1) panels(heteroscedastic)
7	Stata	command = xtgls options = corr(ar1) panels(correlated)
8	Stata	command = xtpcse options = corr(ar1)
9	EViews	GLS Weights = Cross-section weights Coef covariance method = White cross-section
10	EViews	GLS Weights = Cross-section weights Coef covariance method = White period
11	EViews	GLS Weights = Cross-section weights Coef covariance method = White (diagonal)

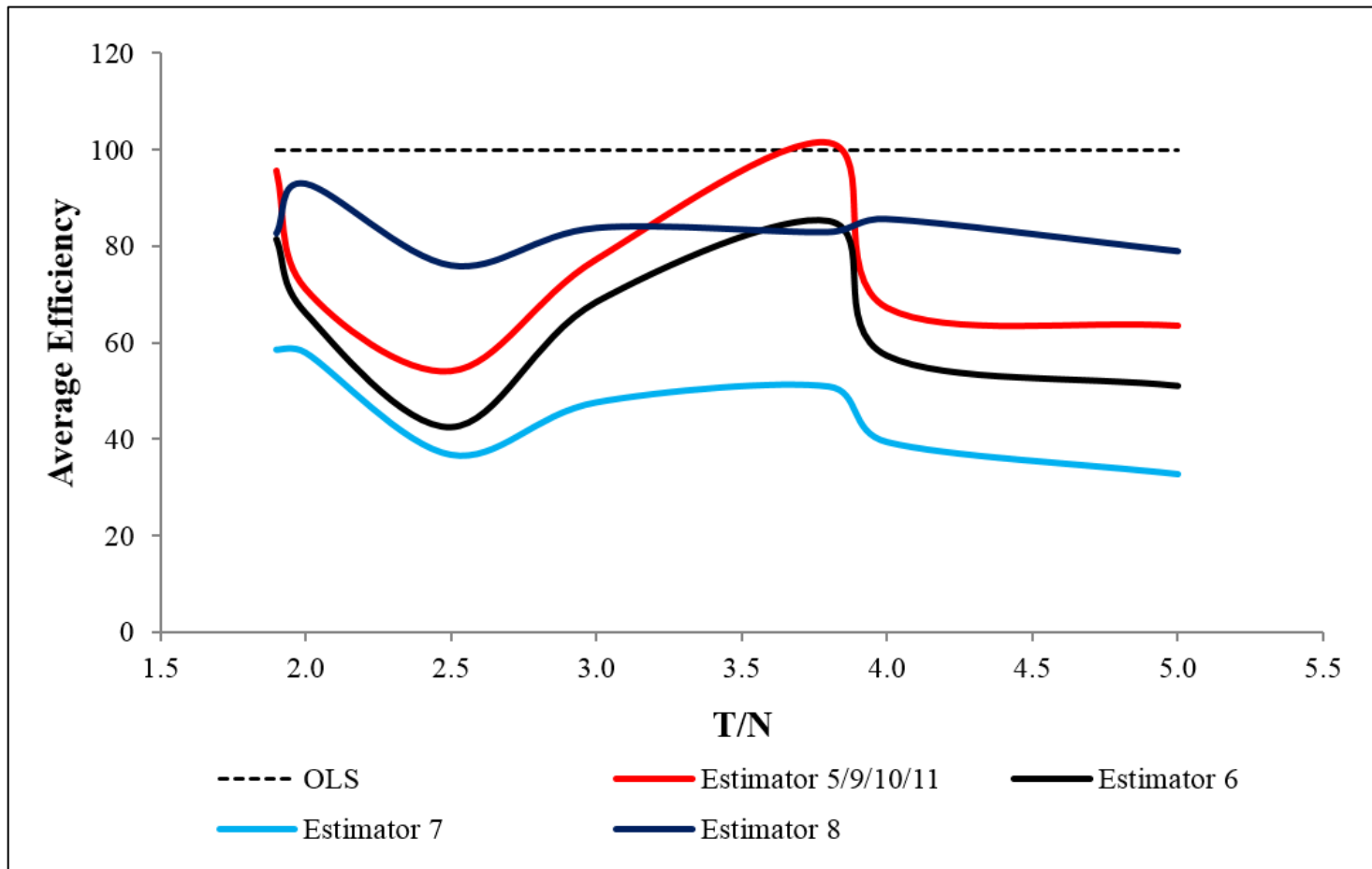
SOURCE: Table 1 in Reed and Ye (2011).

FIGURE 1
Comparison of Estimator *EFFICIENCY*: Reed and Ye (2011) Datasets, $T/N > 1.5$



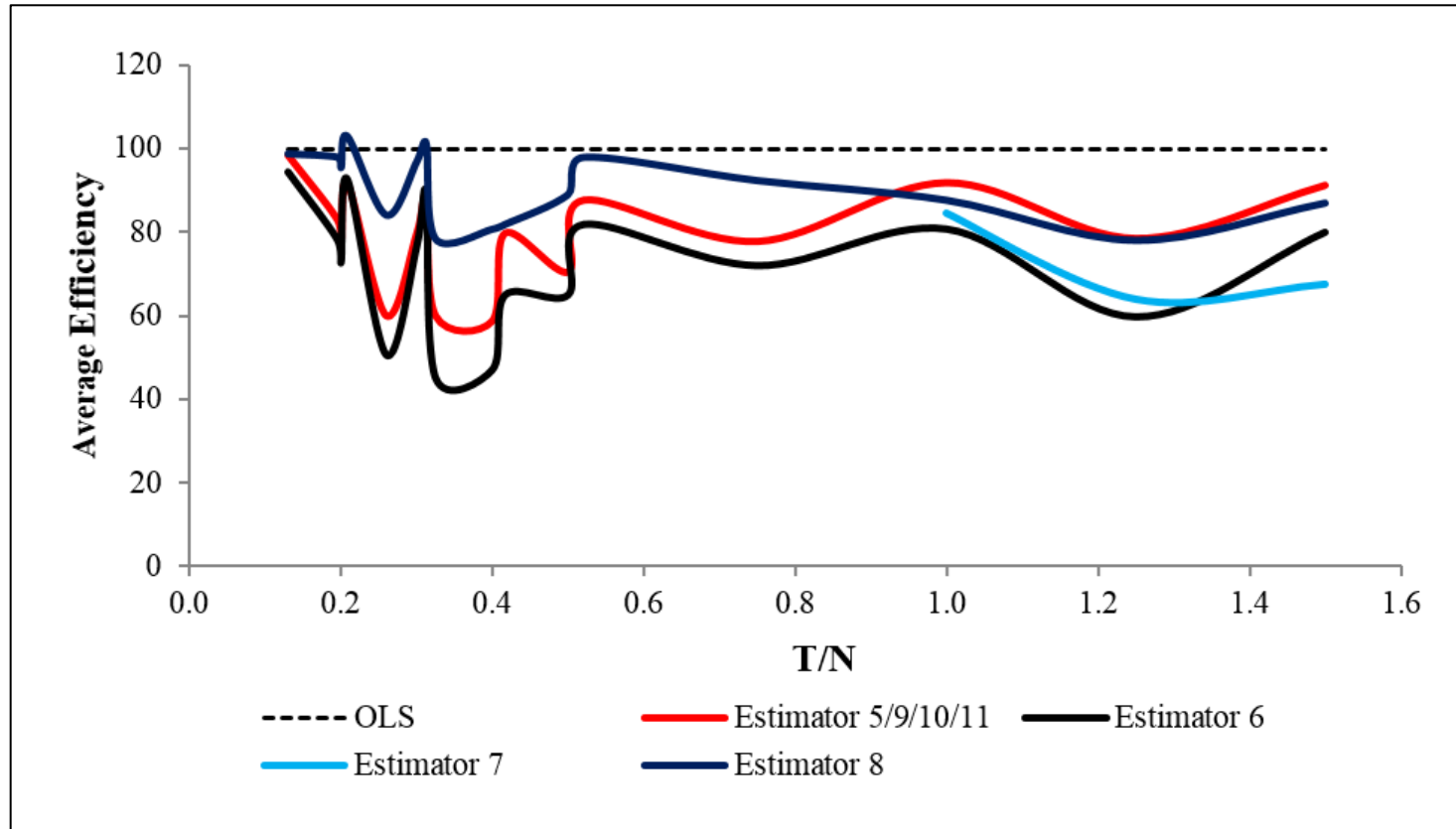
NOTE: The *EFFICIENCY* measure is defined in Section 2 in the text. Estimators are identified in TABLE 3.

FIGURE 2
Comparison of Estimator *EFFICIENCY*: New Datasets, $T/N > 1.5$



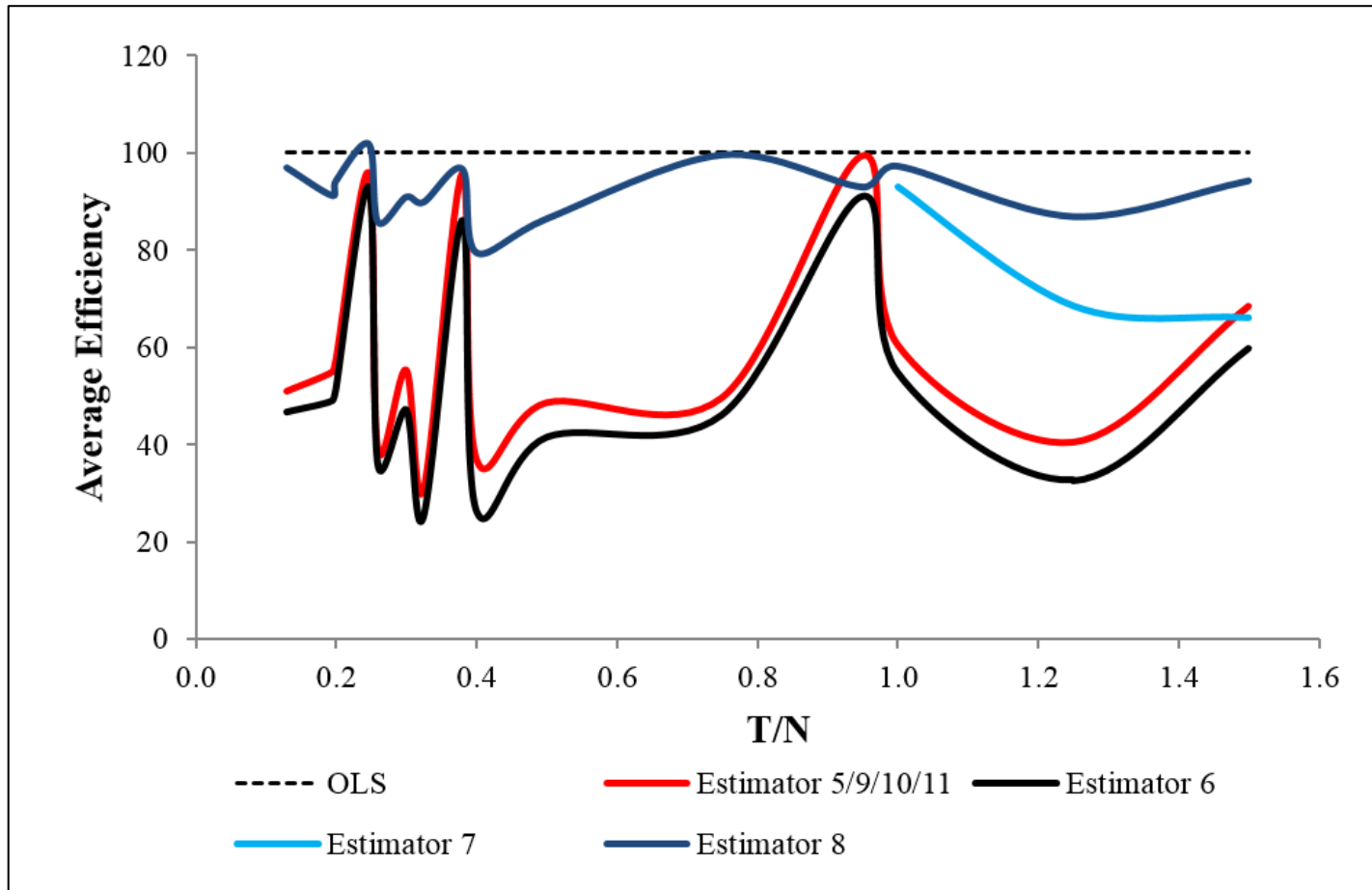
NOTE: The *EFFICIENCY* measure is defined in Section 2 in the text. Estimators are identified in TABLE 3.

FIGURE 3
Comparison of Estimator *EFFICIENCY*: Reed and Ye (2011) Datasets, $T/N \leq 1.5$



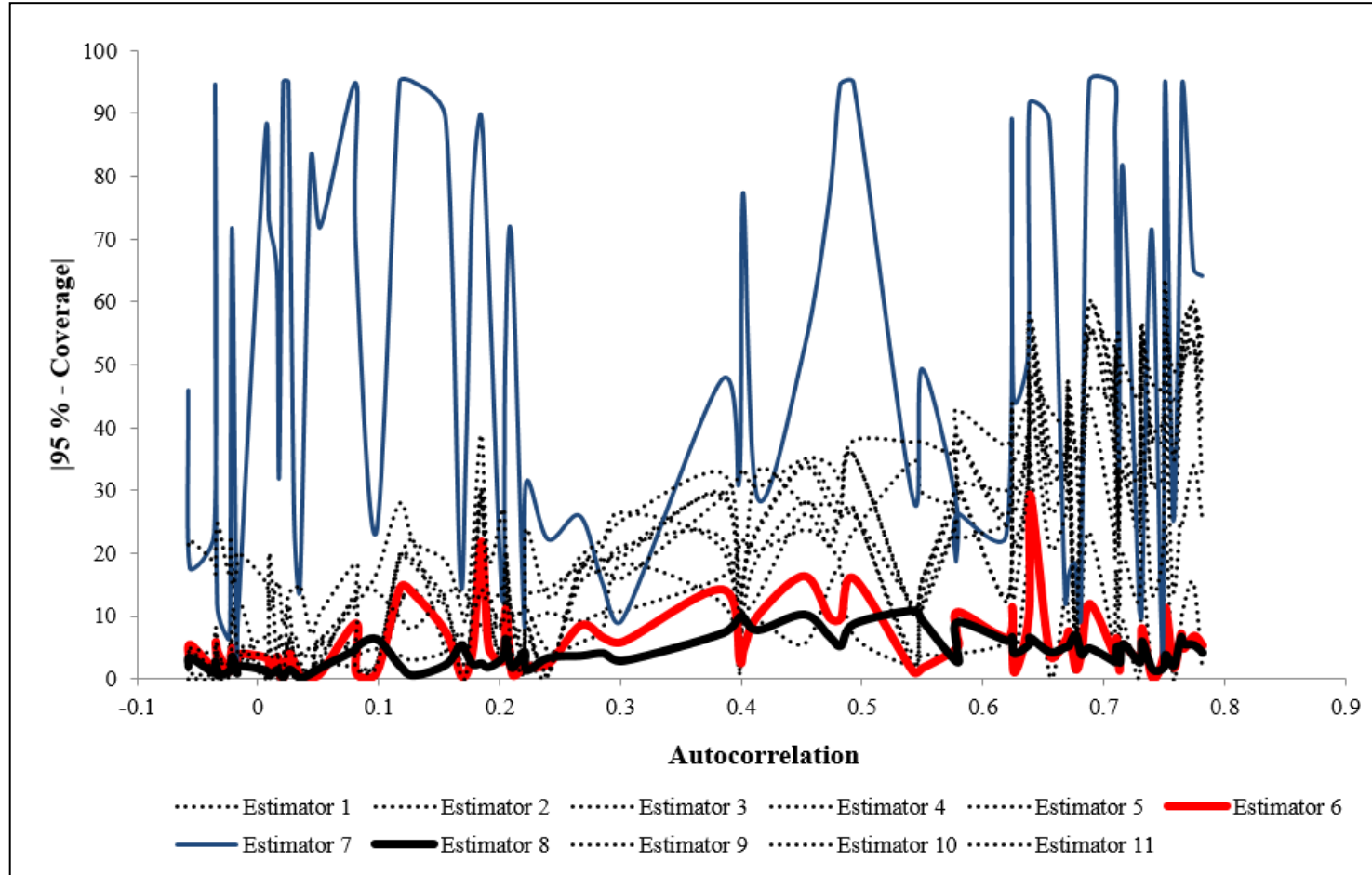
NOTE: The *EFFICIENCY* measure is defined in Section 2 in the text. Estimators are identified in TABLE 3.

FIGURE 4
Comparison of Estimator *EFFICIENCY*: New Datasets, $T/N \leq 1.5$



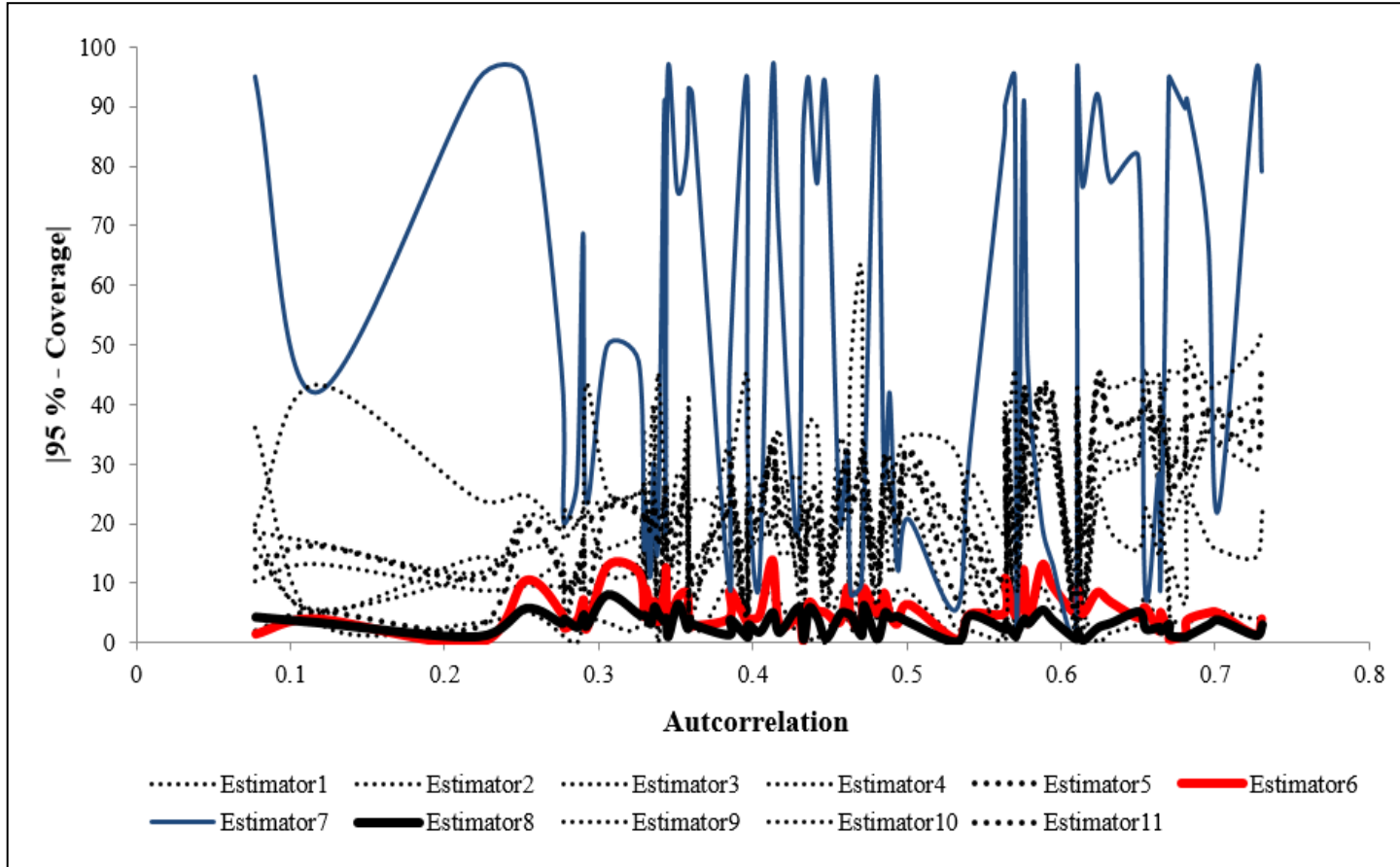
NOTE: The *EFFICIENCY* measure is defined in Section 2 in the text. Estimators are identified in TABLE 3.

FIGURE 5
Comparison of | 95 – Coverage | Values: Reed and Ye (2011) Datasets, $T/N \geq 1.0$



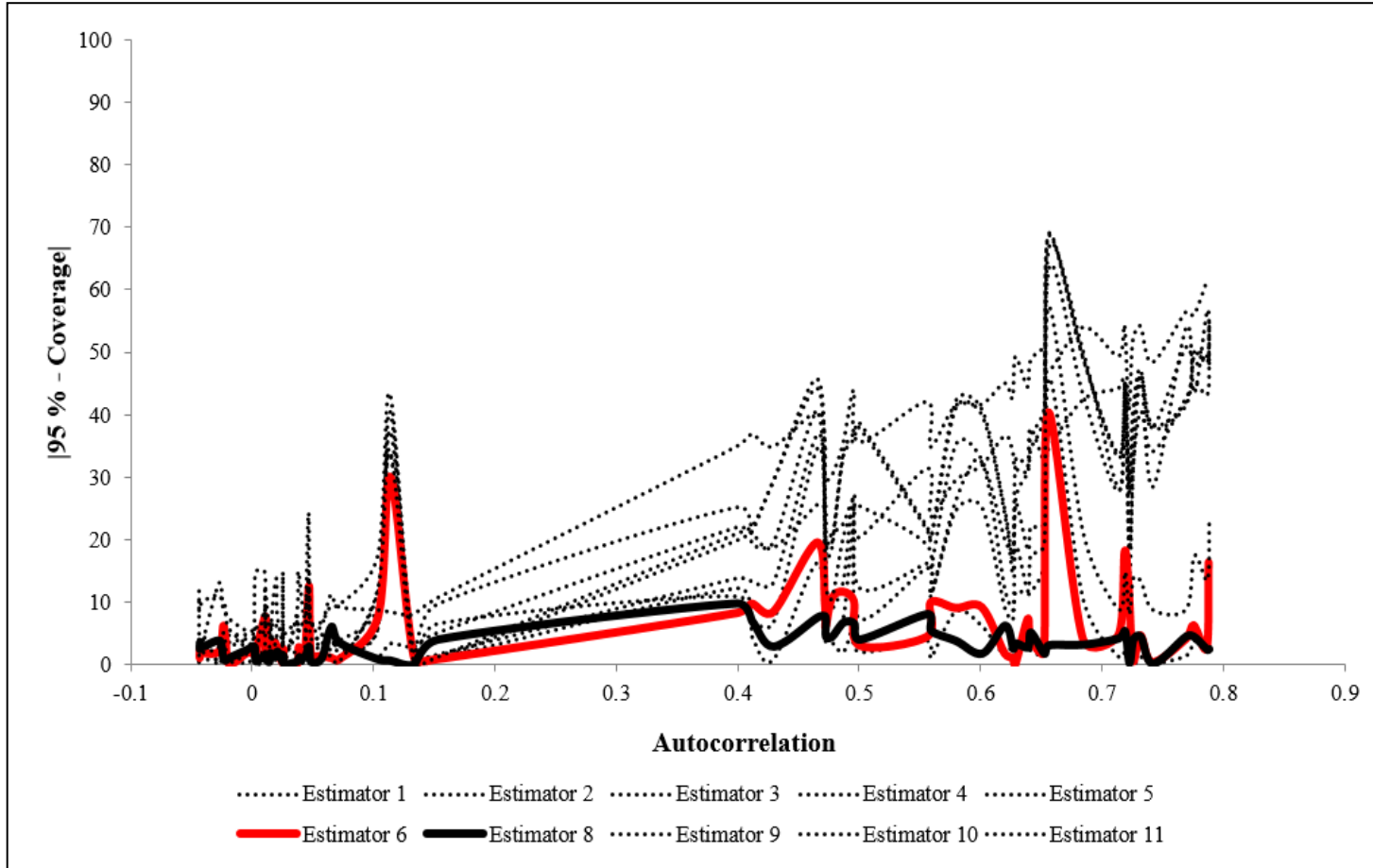
NOTE: The performance measure $|95 - \text{Coverage}|$ is defined in Section 2 in the text. Estimators are identified in TABLE 3.

FIGURE 6
Comparison of $|95 - \text{Coverage}|$ Values: New Datasets, $T/N \geq 1.0$



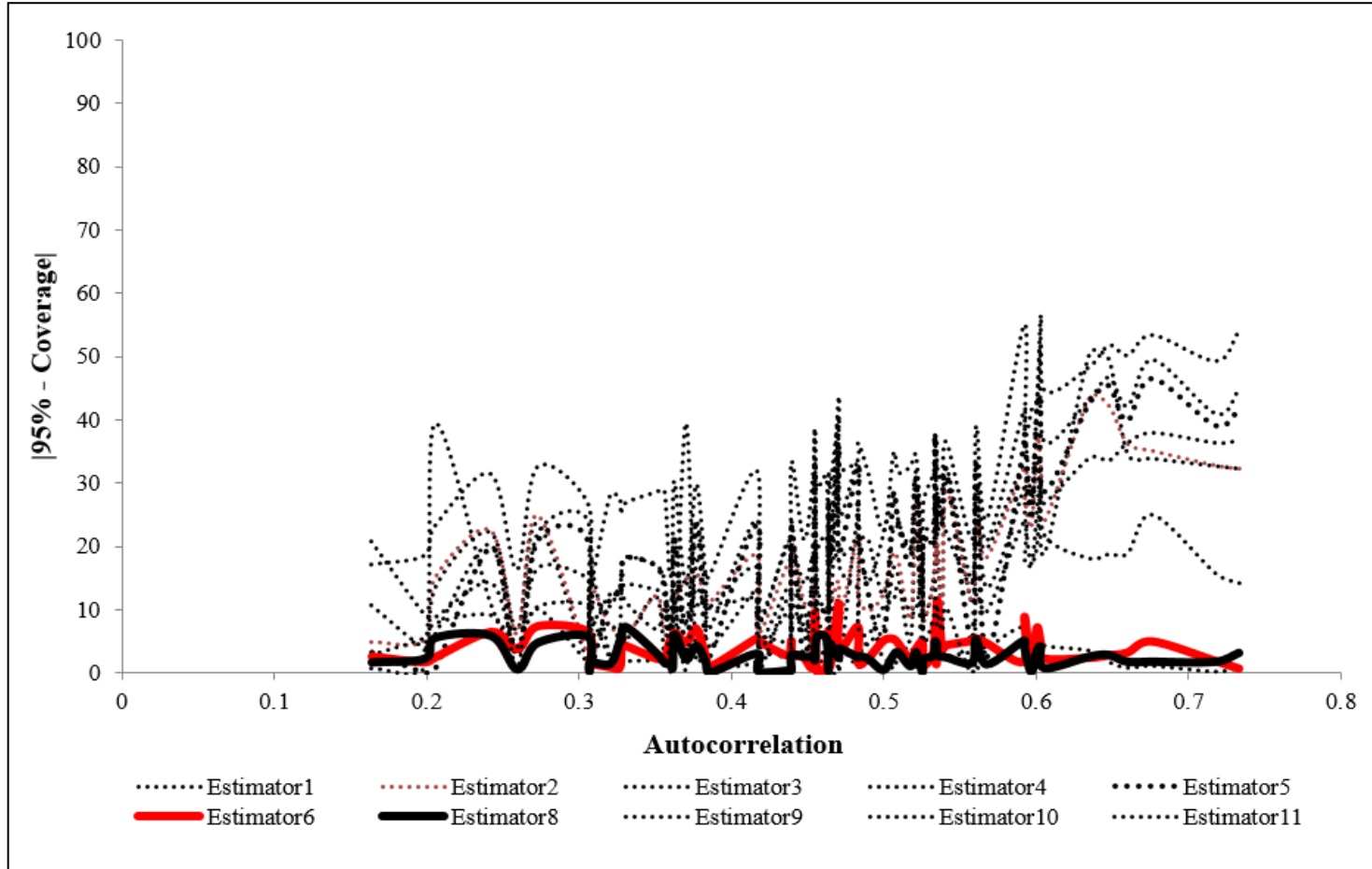
NOTE: The performance measure $|95 - \text{Coverage}|$ is defined in Section 2 in the text. Estimators are identified in TABLE 3.

FIGURE 7
Comparison of | 95 – Coverage | Values: Reed and Ye (2011) Datasets, $T/N < 1.0$



NOTE: The performance measure $|95 - \text{Coverage}|$ is defined in Section 2 in the text. Estimators are identified in TABLE 3.

FIGURE 8
Comparison of $|95 - \text{Coverage}|$ Values: New Datasets, $T/N < 1.0$



NOTE: The performance measure $|95 - \text{Coverage}|$ is defined in Section 2 in the text. Estimators are identified in TABLE 3.